

LETTERS TO THE EDITOR

REACTION RATES OF $C^{12}(\alpha, \gamma)^{16}O$ REACTION AFFECTING SCREENING EFFECT

A. E. MD. KHAIROZZAMAN
B. N. College, Dhubri (Assam)

$C^{12}(\alpha, \gamma)^{16}O$ REACTION rates have been calculated considering screening effect after Mitler⁵, Itoh *et al.*⁴ and Van Horn and Salpeter⁶. The carbon-carbon interaction rates have been found to bring modification to the duration of destruction of carbon to form iron group of elements in carbon detonation supernova.

Introduction

Once carbon is formed by triple alpha reaction, it is destroyed by (α, γ) reaction to yield ^{16}O and so on. Burbidge *et al.*¹ considered these reactions in giant stage of stellar evolution and calculated the reaction rates without considering the screening effect. The work of Duorah³ can also be improved.

After exhaustion of helium, further gravitational contraction leads to higher temperature. At $T_9 = 0.8$, C^{12} may react with C^{12} and at about $T_9 = 1$, ^{16}O may react with ^{16}O in carbon-oxygen degenerate core. The $C^{12}(\alpha, \gamma)^{16}O$ is the reaction to synthesise Ne^{20} , Mg^{24} , etc., while carbon-carbon interaction leads ultimately to the formation of iron group of elements.

The non resonant $C^{12}(\alpha, \gamma)^{16}O$ reaction

This reaction takes place at a temperature of the order 10^8 K and density 10^5 g cm^{-3} . We use here the dimensionless parameter, Γ introduced by Van Horn and Salpeter⁶

$$\Gamma = \frac{z^2 e^2}{aKT} \tag{1}$$

where

$$a = \text{mean ionic distance} = \left(\frac{3}{4\pi n_e}\right)^{1/3}$$

For helium plasma,

$$n_e = 2n_a = 2 \left[\frac{\rho N_A X_a}{A_a} \right] \text{ cm}^{-3}$$

Taking $\rho X_a = 10^5$ gm/cc, we get,

$$n_a = 1.507 \times 10^{26} \text{ cm}^{-3} \text{ and } a = 10^{-26}/12.56 \text{ cm}.$$

Putting n_e and 'a' from the above and $K = 1.38 \times 10^{-16}$ erg/K in the expression (1), we get $\Gamma \ll 1$. Hence it is in weak screening regime. We take the well known enhancement factor in weak screening regime to be $\text{Exp}\{3^{1/2} \Gamma^{3/2}\}$ from Itoh *et al.*⁴,

The unscreened non resonant reaction rate per particle of type 2 with type 1 is taken from Burbidge *et al.*¹

$$\rho_{nr} = 4.34 \times 10^5 \frac{\rho X_1}{A_1} (AZ_1Z_2)^{-1} \tau^2 e^{-\tau} \text{ sec}^{-1} \tag{2}$$

The screened reaction rate thus becomes equal to

$$\rho_{nr} = 4.34 \times 10^5 \frac{\rho X_1}{A_1} (AZ_1Z_2)^{-1} \tau^2 e^{(-\tau + 3^{1/2} \Gamma^{3/2})} \times \text{sec}^{-1} \tag{3}$$

The cross-section factor, S is given by

$$S = \sigma E \exp(31.28 z_0 z_1 A^{1/2} E^{-1/2}) \text{ keV gams.} \tag{4}$$

In this expression σ is the reaction cross-section in barns and E is the particle energy in centre of mass system in KeV. σ 's can be found by usual method

$$E = 26.28 (z_0^2 z_1^2 A T_9^2)^{1/3} \text{ KeV.} \tag{5}$$

τ in the equation (3) is given by

$$\tau = 19.72 (z_0^2 z_1^2 A)^{1/3} T_9^{-1/3}. \tag{6}$$

After, finding the reactions rates by the above equations at temperatures from 10^8 K to 2×10^8 K, the mean life in years (inverse of the rate of destruction) has been found at density, 10^5 g cm^{-3} .

From Table I, we observe that the decrease of mean life in years due to the screening effect is meagre as the screening effect does not augment the reactions much. We add in passing that when Γ is much less than 1, the screening effect of electron cloud have but little effect. If we consider situations in carbon detonation supernova, the density and temperature would be quite large and strong screening will be

TABLE I

Logarithm of mean life (+ in years) in helium burning reactions at $\rho X_a = 10^5$ gm/cc

T_9	Γ	$C^{12}(\alpha, \gamma)^{16}O$ rate without screening	$C^{12}(\alpha, \gamma)^{16}O$ rate with screening	Pycno-nuclear rate of Camaron ² for compariso
1	.292	7.57	7.45	6.32
1.2	.243	5.94	5.85	4.32
1.6	.182	4.09	4.03	2.30
2	.146	1.91	1.87	..